

Ex: 3 Given:  $f(x) = x^2$  &  $g(x) = x - 3$   
 Find  $(f \cdot g)(x)$

$$(f \cdot g)(x) = (x^2)(x-3)$$

$$= x^3 - 3x^2$$

Ex: 4 Given:  $f(x) = \sqrt{x}$   $g(x) = \sqrt{4-x^2}$

$$\text{find } (f/g)(x) = \frac{\sqrt{x}}{\sqrt{4-x^2}} \rightarrow x \neq \pm 2$$

$$\begin{aligned} 4 - x^2 &= 0 \\ \sqrt{4} &= \sqrt{x^2} \\ \pm 2 &= x \end{aligned}$$

### Composition of Functions

$$(f \circ g)(x) = f(g(x))$$

$$(g \circ f)(x) = g(f(x))$$

Ex: 6 Given:  $f(x) = x + 2$   $g(x) = 4 - x^2$

a) Find  $(f \circ g)(x) = (4-x^2) + 2$

$$= 4 - x^2 + 2$$

$$(f \circ g)(x) = 6 - x^2$$

b) Find  $(g \circ f)(x) = 4 - (x+2)^2$

$$= 4 - (\overbrace{x^2 + 4x + 4})$$

$$= 4 - x^2 - 4x - 4$$

$$= -x^2 - 4x$$

c) Find  $(g \circ g)(x) = 4 - (4-x^2)^2$

$$= 4 - (\overbrace{16 - 8x^2 + x^4})$$

$$= 4 - 16 + 8x^2 - x^4$$

$$(g \circ g)(x) = -x^4 + 8x^2 - 12$$